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# CSTNU Tool: A Java library for checking temporal networks

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## ABSTRACT

This paper presents *CSTNU Tool*, a Java library for representing and checking different kinds of temporal constraint networks. In particular, *CSTNU Tool* offers an optimized implementation of some constraint-propagation algorithms to check the dynamic consistency/controllability (DC) of *Conditional Simple Temporal Networks (CSTNs)*, *Conditional Simple Temporal Networks with Uncertainty (CSTNUs)*, and *Flexible Simple Temporal Networks with Uncertainty (FTNUs)*. The optimization is with respect to the management of labeled values that are present in conditional and flexible networks.

The library offers also a simple GUI application to build/manage and check temporal networks in an intuitive way, and some Java programs for generating random temporal networks according to some input parameters.

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## Code metadata

Current code version	4.3
Permanent link to code/repository used for this code version	<a href="https://github.com/ElsevierSoftwareX/SOFTX-D-21-00153">https://github.com/ElsevierSoftwareX/SOFTX-D-21-00153</a>
Code Ocean compute capsule	<a href="https://codeocean.com/capsule/7405126/">https://codeocean.com/capsule/7405126/</a>
Legal Code License	LGPL-3.0-or-later, CC0-1.0
Code versioning system used	SVN
Software code languages, tools, and services used	Java. Bash for utility scripts (not necessary)
Compilation requirements, operating environments & dependencies	Java ≥ 11
If available Link to developer documentation/manual	<a href="https://profs.scienze.univr.it/posenato/svn/sw/CSTNU/trunk/README.md">https://profs.scienze.univr.it/posenato/svn/sw/CSTNU/trunk/README.md</a>
Project web site	<a href="https://profs.scienze.univr.it/~posenato/software/cstnu/">https://profs.scienze.univr.it/~posenato/software/cstnu/</a>
Support email for questions	<a href="mailto:roberto.posenato@univr.it">roberto.posenato@univr.it</a>

## Software metadata

Current software version	4.3
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Legal Software License	LGPL-3.0-or-later, CC0-1.0
Computing platforms/Operating Systems	Unix-like, Linux, OS X, Microsoft Windows
Installation requirements & dependencies	Java ≥ 11
If available, link to user manual	<a href="http://profs.scienze.univr.it/~posenato/software/cstnu">http://profs.scienze.univr.it/~posenato/software/cstnu</a>
Support email for questions	<a href="mailto:roberto.posenato@univr.it">roberto.posenato@univr.it</a>

## 1. Motivation and significance

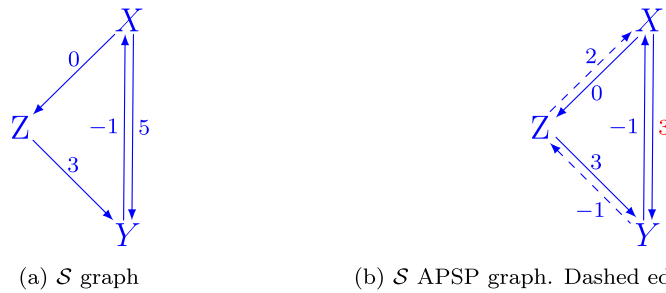
Constraint-based temporal reasoning has been widely used in some applications across heterogeneous domains [1]. Over the

years, different proposals have been presented to address specific requirements that frequently arise in real-world applications.

The most commonly used formalism is the *Simple Temporal Network (STN)* model, in which a set of real-valued variables, called *time-points*, are subject to binary difference constraints [2]. Time-points represent the occurrence of events while binary difference constraints represent the minimal/maximal allowed distance between pairs of events.

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URL: <https://www.di.univr.it/?ent=persona&id=102>.



(a)  $\mathcal{S}$  graph

(b)  $\mathcal{S}$  APSP graph. Dashed edges are added by the Floyd-Warshall algorithm. The red value is the new value for the original constraint  $Y - X \leq 5$ .

Fig. 1.  $\mathcal{S}$  graph representations.

**Example 1.** Let  $\mathcal{S}$  be an STN defined by time-points  $X$ ,  $Y$ , and  $Z$  and the following temporal constraints

$$\begin{aligned} Y - X &\leq 5 \\ X - Y &\leq -1 \\ Z - X &\leq 0 \\ Y - Z &\leq 3 \end{aligned}$$

Usually,  $Z$  is a special time-point that represents the first executed time-point and whose value is fixed at 0. In this way, expression like  $Z - X \leq 0$  and  $Y - Z \leq 3$  can be simplified as unary constraints  $X \geq 0$  and  $Y - Z \leq 3$ , respectively.

Therefore,  $\mathcal{S}$  represents the fact that the temporal distance between  $Y$  and  $X$  must be in  $[1, 5]$ , the distance between  $Y$  and  $Z$  must be in  $[0, 3]$ , and the distance between  $X$  and  $Z$  must be non-negative.

The main problem regarding STN is the *consistency* problem, i.e., to check if an STN admits time-point assignments that satisfy all temporal constraints of the network.

An efficient way to represent an STN is to use a graph, called *STN/distance graph*, where vertices represent time-points and edges represent binary constraints, i.e., an edge  $X \xrightarrow{\delta} Y$  represents the constraint  $Y - X \leq \delta$  [2]. Given an STN, checking its consistency is equivalent to determine all-pairs-shortest-paths (APSP) matrix of its graph using an algorithm like Floyd-Warshall or Johnson [2]: the STN is consistent if and only if the main diagonal of ASPSP matrix is non-negative, i.e., there is no negative cycle in the graph. Moreover, since the APSP matrix contains the minimal distances between any pair of time-points, the corresponding graph represents the minimal STN graph equivalent to the original one.

**Example 2.** Fig. 1(a) shows the graph associated to the previous  $\mathcal{S}$ . Fig. 1(b) depicts the APSP graph obtained executing Floyd-Warshall algorithm. Dashed edges represent the implicit constraints obtained propagating the original constraints. As regards constraint  $X \xrightarrow{5} Y$ , the algorithm determines that the constraint must be restricted to value 3 because values in  $(3, 5]$  are not admissible by other constraints.

Beyond STNs, a significant amount of research has focused on temporal reasoning in the presence of uncertainty. Temporal uncertainty arises, for example, when the duration of some activities can be only observed in real-time by the executor of the network. A *contingent link* represents an interval whose duration is bounded but uncontrollable, i.e., its value is decided by an external agent during execution; Usually, a contingent link between two time-points  $X$  and  $Y$  is represented as  $(X, [l, u], Y)$ , where  $l$  and  $u$  are real values and range  $[l, u]$  represents the possible durations of the contingent link.  $X$  is set (or, equivalently, is executed)

by the executor of the network while  $Y$  is only observed once the external agent executes it.  $Y$  is said *contingent* time-point. An STN containing contingent links is called a *Simple Temporal Network with Uncertainty (STNU)* [3]. In STNUs, the consistency problem is replaced by the *dynamically controllable (DC)* problem, i.e., to check if there exists a strategy for executing the non-contingent time-points such that all constraints are guaranteed to be satisfied no matter how the durations of the contingent links turn out during execution [4].

Example of possible applications of STNU are in the field of robot control [5], web-services compositions [6], and business processes [7,8].

**Example 3.** Fig. 2(a) shows the graph associated to the STNU  $\mathcal{S}'$  defined by time-points  $X$ ,  $Y$ , and  $Z$ , the contingent link  $(X, [1, 5], Y)$ , and the following temporal constraints

$$\begin{aligned} Z - X &\leq 0 \\ Y - Z &\leq 3. \end{aligned}$$

The representation of a contingent link using edges was proposed by Morris and Muscettola [9]: the upper bound of the contingent range is represented as  $Y \xrightarrow{(Y:-5)} X$ , called *upper-case (label) constraint*, while the lower bound is represented as  $X \xrightarrow{(Y:1)} Y$ , called *lower-case (label) constraint*. Upper-case constraints can be propagated assuming the meaning of *wait* constraints. For example,  $D \xrightarrow{(Y:-10)} X$  means that “ $D$  must wait the occurrence of  $Y$  or at least 10 units after the execution of  $X$  for being executed”. Morris and Muscettola determined the first polynomial-time DC checking algorithm for STNU [9]. It can be viewed as an extension of the Floyd-Warshall algorithm in which also upper/lower case constraints are considered/propagated. Then, many other propagation-based algorithms have been proposed to make the DC check even faster [9–16].

The above  $\mathcal{S}'$  is not dynamic controllable. Indeed, contingent link  $(X, [1, 5], Y)$  guarantees that  $Y$  can occur 5 units after the occurrence of  $X$  while constraint  $Y \leq 3$  requires that  $Y$  must occur within 3 units after  $Z$ . Since  $X$  cannot be executed before  $Z$ , it is not possible to guarantee that  $Y$  can occur at any admissible time  $(3, 5]$  after  $X$  without violating the constraint  $Y \leq 3$ . Fig. 2(b) shows the graph obtained by the execution of Morris and Muscettola DC checking algorithm [9]. The wait  $X \xrightarrow{(Y,-2)} X$  is equivalent to a negative loop in STNs, i.e.,  $\mathcal{S}'$  is not dynamic controllable.

Although STNUs have been successful in some domains, other domains require also constraints with condition. For example, in the health-care domain, medical tests on a patient frequently generate information in real-time that can affect which pathway that patient will follow [17]. Different pathways have different set



(a)  $S'$  graph where the contingent link is represented by an upper-case constraint (red) and a lower-case one (red).

(b) Negative loop in  $S'$  graph determined by Morris-Muscettola DC checking algorithm [9].

Fig. 2.  $S'$  graph and its derived graph.

of constraints. It has to be guaranteed that any possible execution of the temporal network strictly satisfies all specified temporal constraints no matter which test outcomes are observed. The *Conditional Simple Temporal Network (CSTN)* model allows the representation of temporal constraints in conjunction with scenarios [18].

In detail, in a CSTN there can be *boolean observations*  $p, q, r, s, \dots$ , each of them is associated to a proper time-point, called *observation time-point*. During an execution, when an observation time-point is executed, e.g.,  $P?$ , then the associated boolean observation, e.g.,  $p$ , is set to  $\top/\perp$  by the environment.

A conjunction of some literals of the boolean observations is called (*propositional*) *label*. A label is  $\top$  if and only if all its literal are  $\top$  after that all observations have been set. A complete assignment of the observations of a CSTN is a *scenario*.

For example, label  $p \rightarrow q$  is true if and only if after the execution of the corresponding observation time-points,  $p = \top$  and  $q = \perp$ .

Each constraint in a CSTN may be associated to a label that represents the *condition* for considering the constraint. For example,  $X \xrightarrow{\langle \delta, p \rightarrow q \rangle} Y$  represents the constraint  $Y - X \leq \delta$  that must be satisfied in all *scenarios* in which  $p \rightarrow q$  is  $\top$ .

It is possible to have more conditional constraints between the same pair of time-points, each of them having a different label. Therefore, a CSTN graph can be a multi-graph.

As shown in [19], it is more efficient to represent the possible different conditional constraints between a pair of time-points as one constraint with a set of labeled values because it is possible to maintain minimal the size of such a set by applying a set of minimization rules derived from Assumption-based Truth Maintenance Systems (ATMS) [19]. For example, if in a CSTN network there are the boolean observation  $p$  and  $q$ , the edge  $X \xrightarrow{\langle (10, p \rightarrow q), (4, q) \rangle} Y$  represents two constraints:

1.  $Y - X \leq 10$  that must be satisfied in scenario where  $p \rightarrow q$  is  $\top$ , and
2.  $Y - X \leq 4$  that must be satisfied in scenarios where  $q$  is  $\top$ .

Adding the labeled value  $\langle 4, \neg q \rangle$  to the edge, it results that the constraint  $\leq 4$  must be considered in all scenarios ( $q \vee \neg q \equiv \top \equiv \square$ ), and it is the most restrictive in the set. Therefore, the edge can be simplified as  $X \xrightarrow{\langle 4, \square \rangle} Y$ .

A CSTN is said to be *dynamically consistent (DC)* if it admits a strategy that, reacting to the past observation, guarantees the satisfaction of all relevant constraints no matter which outcomes are observed during execution.

According to the delay by which an executor can acquire the value of observations, there are different kinds of dynamic consistency. For example, the Instantaneous Reaction (IR) assumption says that an executor can react instantaneously when an observation is set executing a time-point at the same instant if it is necessary; the  $\varepsilon$ -DC says that an executor can react after a delay  $\varepsilon > 0$ . In [20] there is a survey of the different kinds of dynamic consistency and their relations.

In the literature, there are different DC checking algorithms for CSTNs based on the conditional constraint propagation [18, 20–25].

**Example 4.** Fig. 3(a) shows the graph associated to the CSTN  $S''$  defined by time-points  $P?, Y$ , and  $Z$ , with  $P?$  observation time-point of  $p$ , and the following conditional temporal constraints

$$\begin{aligned} Y - P? &\leq 5, \neg p \\ P? - Y &\leq -6, p \\ Z - P? &\leq 0, \square \\ Y - Z &\leq 3, \neg p \end{aligned}$$

Fig. 3(b) depicts the graph after the execution of the Hunsberger–Posenato DC checking algorithm [20].  $S''$  is DC. The cycle between  $P?$  and  $Y$  is not a negative cycle because the two constraints are not in the same scenarios. The algorithm determines the minimal constraints for an early-execution strategy. Considering the edges from time-points to  $Z$ , it is possible to determine the dynamic scheduling:  $Z$  and  $P?$  must be executed at 0; at the execution of  $P?$ ,  $p$  is set; then,  $Y$  must be executed at 0 if  $p = \perp$ , at 6 otherwise.

The *Conditional Simple Temporal Network with Uncertainty (CSTNU)* model extends the CSTN one allowing the representation of contingent links [26–30]. Fig. 5 depicts an interesting CSTNU instance where there are 3 contingent links and some conditional constraints that determine when activate such contingent link according to the  $p$  value.

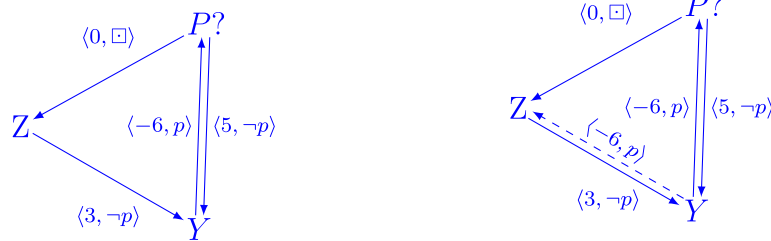
The *Flexible Simple Temporal Networks with Uncertainty (FTNU)* model, also known as Conditional Simple Temporal Network with Partially Shrinkable Uncertainty (CSTNPSU), extends the CSTNU model allowing each contingent link to be partially shrunk at design/execution time [31–33]. The idea is to allow the representation of an ideal duration range of a task that can be partially modified before the start of the task if this permits to satisfy network constraints.

In detail, in FTNUs contingent links are represented as *guarded links*. A guarded link  $(X, [[l, l']][u', u]], Y)$ , with  $0 < l \leq l' \leq u' \leq u < \infty$ , is a “contingent link”  $(X, [l, u], Y)$  that it can be shrunk before its activation, i.e., before  $X$  is executed. The value  $l$  can be raised to  $l'$  at the most, while  $u$  can be decreased to  $u'$  at the most. Let  $l^*, u^*$  the values of  $l, u$ , respectively, when  $X$  is executed. Then, the guarded link becomes a contingent one with range  $[l^*, u^*]$ , and it is activated.

Despite the variety of applications of such models, implementations of methods for solving the consistency/controllability problem cannot be found in publicly available libraries.

The CSTNU Tool library<sup>1</sup> focuses on the solution of the consistency/controllability problem for the above-mentioned models

<sup>1</sup> The reason of CSTNU in the name is that CSTNU model was the only one considered in the initial releases.



(a)  $S''$  graph where  $P?$  is the observation time-point of  $p$ .

(b) The  $S''$  graph determined by Hunsberger-Posenato DC checking algorithm assuming IR [20].

Fig. 3.  $S''$  graph and its derived graph.

offering the implementation of different DC checking algorithms for each model. Users can interact with CSTNU Tool in two forms: using classes/methods from the Java package, aimed for advance users; using the integrated graphical editor to create/modify, and check a temporal constraint network easily, aimed for beginners.

## 2. CSTNU Tool: Software description

### 2.1. Software architecture

The CSTNU Tool is a Java library that runs in any JVM  $\geq 11$ . The library is composed by two main packages: `it.univr.di.labeledvalue` and `it.univr.di.cstnu`.

Package `it.univr.di.labeledvalue` contains classes for representing and managing set of labeled values.

Package `it.univr.di.cstnu` contains classes for representing and managing some kinds of temporal constraint networks. It is divided in three sub-packages: `graph`, `algorithms`, and `visualization`. The `graph` sub-package contains classes for managing the graph of a temporal constraint network where nodes/edges can contain sets of labeled values. The `algorithms` sub-package is the core of the library; it contains a class for each kind of considered temporal constraint network that allows representing and checking of temporal constraint network instances. Moreover, it contains two Java programs for generating random CSTNs/STNUs of different types and sizes. The `visualization` sub-package contains the GUI application `TNEditor` to create/modify/visualize and check any kind of the networks mentioned above. The GUI of `TNEditor` is based on `JUNG` library [34].

### 2.2. Software functionalities

Each instance of a temporal constraint network is represented as an object of the corresponding class in `it.univr.di.cstnu.algorithms`. Such an object contains the graph as an object of the class `it.univr.di.cstnu.graph.TNGraph` and some information about how to check the consistency/controllability. The check of the consistency/controllability property is done by the method `checkConsistency()/checkControllability()`. Some classes offer different implementations of consistency/controllability checks. A specific implementation can be selected by a method before calling the check method. To ease the selection of the appropriate combination of checking algorithm, the kind of DC (e.g., *IR*,  $\varepsilon$ , etc.), and some other settings, there are some derived classes where such selection is pre-defined. The consistency/controllability check method always returns an object that describes the final status of the check, some statistics about the execution, and, in case of an inconsistent network, node(s) where an inconsistency was found.

Fig. 4 shows an excerpt of the UML class diagram of the `it.univr.di.cstnu` package where there are the classes for

representing: (1) all kinds of possible temporal constraint networks (framed in blue), (2) result of a consistency/controllability check (framed in green), and (3) loading/saving the graph (framed in orange). Classes framed in violet are the CSTN sub-classes where some settings about the checking algorithm are already fixed.

Table A.1 in Appendix A summarizes the classes and their possible checking methods.

Package `it.univr.di.cstnu.labeledvalue` allows the representation and management of sets of labeled values in their minimal cardinality guaranteeing that each operation on a set has a linear-order computational cost.

## 3. Illustrative examples

We now provide an illustrative example of how to load and check the CSTNU instance shown in Fig. 5.

CSTNU Tool can load/save temporal constraint networks in GraphML format [35]. (In Appendix B, we present how temporal constraint networks are coded in GraphML in CSTNU Tool library.) Therefore, let us assume that the considered CSTNU instance is stored as a GraphML document in the file named "cstnuSoftwareX.cstnu".

The following simple Java program, using the CSTNU Tool library, loads the instance, executes the checks, and prints the result in the console.

```

1 public static void main(String[] args) {
2     File graphSource = new
3     File("cstnuSoftwareX.cstnu");
4     TNGraphMLReader<CSTNUEdge> loader = new
5     TNGraphMLReader<>();
6     TNGraph<CSTNUEdge> graph = null;
7     System.out.print("Loading the network...");
8     try {
9         graph = loader.readGraph(graphSource,
10         EdgeSupplier.DEFAULT_CSTNU_EDGE_CLASS);
11     } catch (IOException |
12     ParserConfigurationException | SAXException e) {
13         System.err.println("Format error in the
14         instance source file: " + e.getMessage());
15         System.exit(1);
16     }
17     System.out.print("done.\nChecking its dynamic
18     controllability...");
19     CSTNU cstnu = new CSTNU(graph);
20     CSTNUCheckStatus checkStatus = null;
21     try {
22         checkStatus =
23         cstnu.dynamicControllabilityCheck();
24     } catch (WellDefinitionException e) {
25         System.err.println("The cstnu instance is not
26         well defined: " + e.getMessage());
27         System.exit(1);
28     }
29     System.out.print("done\n" + checkStatus);
30 }

```

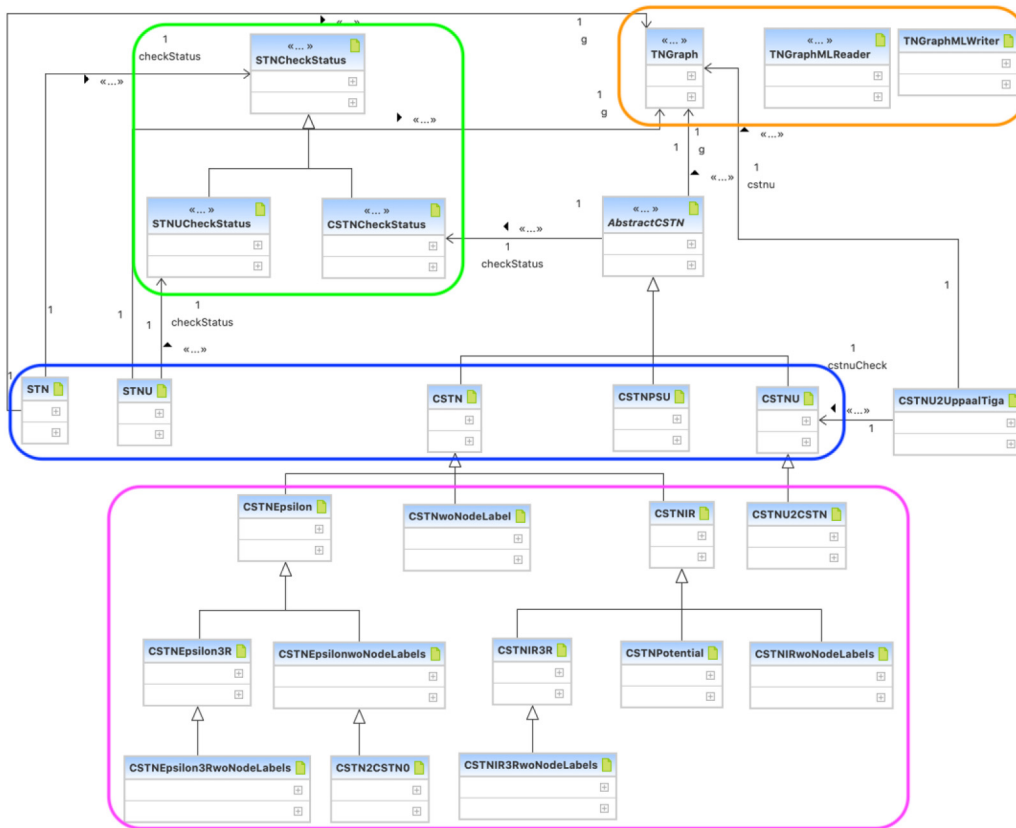


Fig. 4. Excerpt of the UML Class Diagram of the CSTNU Tool library.

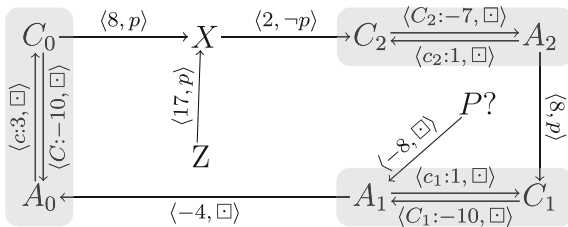


Fig. 5. A CSTNU instance. Constraints in gray regions represent contingent links.

To create an object of the CSTNU class, it is necessary to give the graph representing the network as a constructor parameter. The graph (object of TNGraph<CSTNUEdge>) can be loaded from a file using the helper class TNGraphMLReader (Line 3 and Line 7). Once the CSTNU object is created (Line 13), it is sufficient to call the method checkControllability() to verify the controllability of the instance (Line 16).

The check returns a CSTNUCheckStatus object containing the controllability status of the instance and some other statistics. All the information can be obtained in text form (Line 21). The output of an execution is:

```

Loading the network...done.
Checking its dynamic controllability...done
The check is finished after 3 cycle(s).
The controllability check has determined that given
network is dynamic controllable.
Some statistics:
Rule R0 has been applied 0 times.
Rule R3 has been applied 9 times.
Rule Labeled Propagation has been applied 139 times.
Rule Labeled z! has been applied 30 times.
Rule Labeled Lower Case has been applied 1 times.
Rule Labeled Cross-Lower-Case has been applied 1
times.
    
```

```

Rule Labeled Letter Removal has been applied 12
times.
The global execution time has been 78681000 ns
(~0.07 s)
    
```

The instance results to be controllable. The implemented checking algorithm for CSTNU determines also all constraints that must be considered for a correct execution of the instance and adds them to the graph.

Using the program TNEditor, the checking task is even simpler. Fig. 6 depicts the screenshot of the program after the check of the sample instance has been completed. In general, on the left part of the program window, there is the editor-window where it is possible to load/create/edit a network instance; on the right part, there is the window where the program shows the instance after the execution of one of the different possible manipulating/checking algorithms. The selection of which algorithm to apply is done by the user pushing a button on the command bar present on the lower part of the program window. In the screenshot, the right part shows the completed graph obtained by applying the CSTNU DC-checking algorithm to the sample CSTNU instance, represented on the left part.

#### 4. Impact and conclusions

In this work we described CSTNU Tool, a Java library for analyzing temporal constraint networks. CSTNU Tool offers an efficient implementation of dynamically-controllable/consistent checking algorithms for temporal constraint network models like CSTN, CSTNU, and FTNU.

As regards the impact of the library, it can serve for different purposes to researchers, and in application settings:

- **Applications.** In different fields there is a significant interest in considering temporal aspects for planning, scheduling,

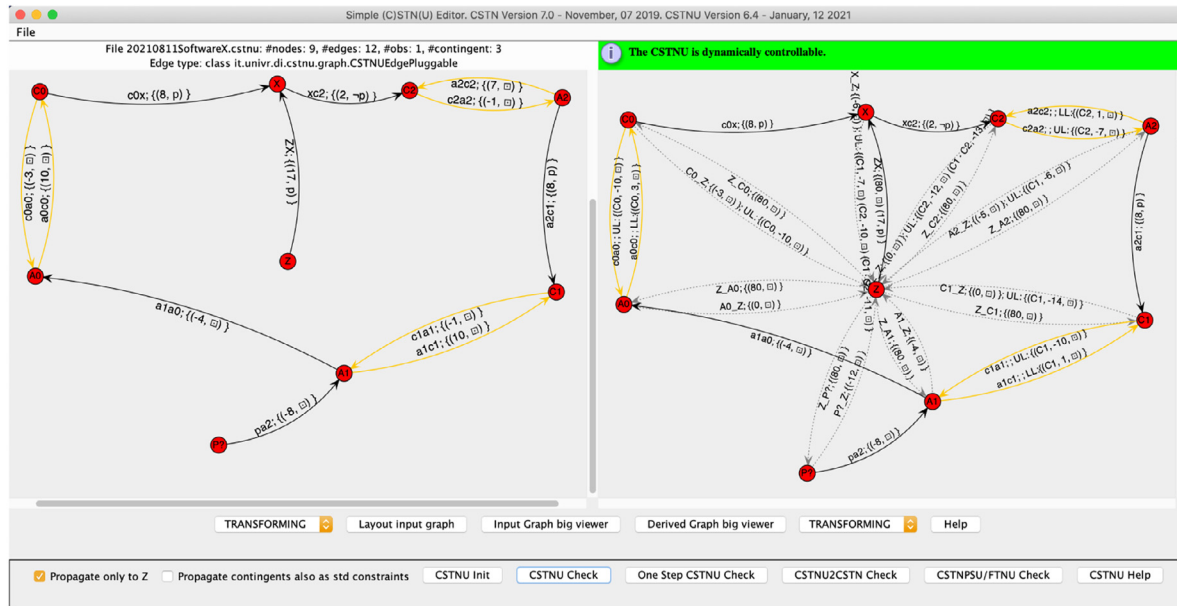


Fig. 6. TNEditor screenshot after the controllability check of the sample instance has been finished.

etc. and making temporal reasoning using temporal constraint networks for their simplicity and “efficiency” with respect other models. For example, in the field of planning/scheduling for robots [19,36–42], and in the field of business processes [32,43–47]. A critical aspect in such systems is the lack of efficient libraries for executing temporal reasoning efficiently. This library would contribute in building efficient solutions for such systems offering efficient algorithms for some temporal constraint network models. The tool has been already considered in [48–50].

- **Introduction to temporal constraint networks.** The GUI TNEditor may help researchers in the study and simulation of temporal constraint networks. For example, the intertwining of conditional constraints and contingent links is not as simple as it seems. TNEditor helps to understand such an intertwining, possible inconsistencies, and how it is possible restore the controllability modifying constraints in a fast way.
- **Test of new checking algorithms.** In the field of temporal reasoning, temporal constraint networks like STN/STNU represent an interesting model because they admit solving some problems efficiently. Although for richer models like CSTN such an efficiency is not possible [51], some researches have shown that some CSTN DC checking algorithms are practically efficient in many benchmarks [20,25]. The algorithms in CSTNU Tool library can be used either as a core for more advanced algorithms or as reference for different new algorithms. Page <http://profs.scienze.univr.it/~posenato/software/cstnu/benchmarkWrapper.html> presents the performances of the implemented algorithms in some benchmarks that are freely available.

In future work we plan to integrate CSTNU Tool library with implementations of *feasibility* and *dynamic scheduling* algorithms. Feasibility algorithms solve the problem of finding all inconsistencies. Dynamic scheduling algorithms allow the execution of a network in real-time.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Classes and possible checking methods

Table A.1 summarizes the classes and their possible checking methods. The full list of the methods and corresponding method parameters is presented in <http://profs.scienze.univr.it/~posenato/software/cstnu/apidocs>.

## Appendix B. Representation of temporal constraint network in graphml format

GraphML is an XML application for representing graphs of different types [35] in a very flexible way. It consists of two parts: a language core to describe the structural properties of a graph, and a flexible extension mechanism to add application-specific data.

In the language core, there are the elements `graph`, `node`, and `edge` by which it is possible to describe the topology of a graph.

The *GraphML-Attributes* extension allows the definition of node/edge attributes in the same XML document where the graph is defined.

In the CSTNU Tool library, it is assumed that a GraphML document describing a temporal constraint network uses the following attributes (we report here the most significant):

**Table A.1**

Summary of implemented checking algorithms.

Class	Checking algorithm
STN	Floyd–Warshall Bellman–Ford (single sink) Bannister–Eppstein Dijkstra Johnson Yen (single sink) BFCT
STNU	Morris14 RUL– RUL20
CSTN	HPC15 HP16 (for $\epsilon$ -reaction) HP18 (3 rules) HP20 (potential)
CSTNU	HP18 HP18 OnlyToZ CSTNU2CSTN
CSTNPSU (FTNU)	PC20

For the CSTN class, HP18 can be configured to work assuming different kind of reaction of the system with respect to the uncertainty of conditions, i.e., standard- $\epsilon$ - $\pi$ - semantics.

```

<key id="Obs" for="node">
  <desc>Proposition Observed. Value specification:
    [a-zA-F]</desc>
</key>
<key id="Label" for="node">
  <desc>Label. Format: [-[a-zA-F]|[a-zA-F]]+|</desc>
  <default></default>
</key>
<key id="Potential" for="node">
  <desc>Labeled Potential Values. Format: {[('node name',
    'integer', 'label')] +}|</desc>
</key>
<key id="Type" for="edge">
  <desc>Type: Possible values:
    contingent|requirement|derived|internal.</desc>
  <default>normal</default>
</key>
<key id="LowerCaseLabeledValues" for="edge">
  <desc>Labeled Lower-Case Values. Format: {[('node name',
    'integer', 'label')] +}|</desc>
</key>
<key id="UpperCaseLabeledValues" for="edge">
  <desc>Labeled Upper-Case Values. Format: {[('node name',
    'integer', 'label')] +}|</desc>
</key>
<key id="Value" for="edge">
  <desc>Value for STN edge. Format: 'integer'</desc>
</key>
<key id="LabeledValues" for="edge">
  <desc>Labeled Values. Format: {[('integer', 'label')
    ] +}|</desc>
</key>

```

Therefore, for example, to assign the labeled values (8, p) and (6, q) to the edge from node C0 to node X, it is sufficient to add the attribute "LabeledValues" as shown in the following listing:

```

<edge id="c0x" source="C0" target="X">
  <data key="LabeledValues">{(8, p), (6, q)}</data>
</edge>

```

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