

Colossal low-temperature upturn in the heat capacity of volcanic glasses

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ABSTRACT

Here we explore the low-temperature heat capacity (C_p) of two natural endmember volcanic glasses, unveiling an unprecedented anomalous upturn in C_p/T^3 versus temperature (T) dependencies. This distinctive behavior, previously unseen at this scale, obscures the accurate boson peak position, posing a significant analytical challenge. Through rigorous examination, we established the magnetic origin of this anomaly, proved by subjecting the samples to a magnetic field up to 9 Tesla. The investigations uncovered a nuanced interplay between magnetic models, as we sought to provide an explanation for describing this captivating phenomenon.

1. Introduction

The mechanisms governing the eruptive style of volcanoes are deeply connected to the physicochemical properties of magmas. These materials are usually classified as multiphase and multicomponent systems, whose structure controls the dynamics of the magmatic rising [1]. The liquid phase of these systems represents their leading component dominating viscoelastic response and flow behavior [2]. Any magmatic process is unavoidably recorded into the silicate structures of the erupted products and in particular, the glassy fraction records the final moments of an eruption. Following, the study of these enigmatic glasses opened the way to a wide range of methodologies aimed at unveiling their intrinsic structure (*i.e.* short and medium range order) and how it affects their macroscopic response to deformations [3–5]. However, still little is known about their low-temperature heat capacity (C_p). Indeed, its temperature dependence is key in accessing the glass structure and, paradoxically, the high-temperature entropy thus, underpinning deep implications on melt viscosity [6]. Following, the exploration of low- T range of simplified silicate glassy systems suggests that C_p is mostly governed by variations of the structural medium-range order rather than by an additive compositional law [7–9]. However, those investigations were conducted by ruling out an essential component of natural silicate glass: iron. Despite the numerous approaches and methodologies used to unravel its intriguing behavior, the role of iron in the medium- and short-range order of silicate glasses is and remains a standing issue [10]. Here we provide strong evidences of its potential magnetic influence

displayed by a colossal low- T upturn in two end-member natural volcanic glasses: basalt and rhyolite respectively. This anomaly has never been observed or reported in literature in silicate glasses so far. Thus, we also attempted an interpretation of our preliminary results in terms of an additional spin fluctuation contribution [11] or cluster theory [12,13], obtaining a surprising competition between the two approaches in describing the heat capacity data of both samples subjected to a magnetic field.

2. Materials and methods

The investigated volcanic glasses (characterized in Ref. [14,15]) represent two natural sub-alkaline endmembers, basalt (B_{100}) and rhyolite (R_{100}) respectively, whose composition, Fe^{2+}/Fe_{tot} ratio and densities (ρ) are reported in Table 1. The two glasses differ mainly from their content in SiO_2 , and the most relevant element-oxides of the so-called network modifiers group (CaO , MgO , Na_2O , K_2O) and particularly in FeO_{tot} . B_{100} is richer in non-bridging oxygen and iron oxide than R_{100} that shows a much stronger network-connectivity. According to the Raman spectra reported in [15] the R_{100} structure is richer in larger tetrahedral rings (*i.e.* 6-membered rings) with respect to that of B_{100} .

Temperature dependence of heat capacity was determined by a standard thermal relaxation method implemented in the He^4 PPMS system [16]. The measurements were taken for a temperature range from 1.9 K up to 50 K with the magnetic field from 0T to 9T in 1T step.

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The mass of particular samples used in the experiment was: B₁₀₀–10.70 mg and R₁₀₀–8.45 mg.

3. Results and discussions

The characteristics of the low temperature heat capacity of glasses are a linear term contribution and the appearance of the boson peak (BP) which is a result of an excess in the low-frequency THz of the vibrational density of states, universally related to the intrinsic disorder of glasses (see the BP of SiO₂ glass in Fig. 1). The experimental data can be accordingly approximated according to Ref. [17] as:

$$C_p = \alpha T + \beta T^3 + \delta T^5, \quad (1)$$

where αT corresponds to the tunneling between two level states, βT^3 is the Debye contribution present in any solid and δT^5 stems from the soft modes. For a typical C_p/T^3 vs T one should expect a pronounced maximum at the BP temperature and depending on the available temperature range towards the low temperatures an upturn related to the linear term in the Eq. (1). Fig. 1 shows the raw C_p/T^3 vs T results for the R₁₀₀ and B₁₀₀. In order to emphasize the expected traditional glassy picture (BP), the literature data of SiO₂ case are included as solid grey lines [18,19]. The inset in upper left corner shows the experimental data in C_p/T vs T^2 coordinates up to 10 K range.

The BP vicinity is almost undetectable in both volcanic glasses, in R₁₀₀ BP (although very smeared) is still determinable, whilst in B₁₀₀ it is no longer possible. In order to eliminate the unlikely experimental system's influence, additional runs confirming the high accuracy and repeatability of specific heat data, further measurements were performed on a secondary calorimetric cell (not included in the paper) for both samples.

It can be inferred that the real behavior at the lowest temperatures is hidden by a massive contribution from the low temperature range, associated with the linear contribution. To present the enormous extent of this anomalous behavior at lowest temperatures, an additional plot showing the higher values at the Y axis is reported in *Supplementary material*, Figure S1. The distinct temperature dependence is even more pronounced when the experimental data are plotted in the C_p/T vs T^2 form (see inset in Fig. 1). Instead of a simple linear dependence (or lightly parabolic if the soft potential model in the C_p approximation is included) we report a strong “upturn” at temperatures below 4.5 K for R₁₀₀ and 9 K for B₁₀₀. A direct example of this behavior is reported in Ref. [20], where an iron bearing soda-lime glass, loaded with 2 wt.% of Fe₂O₃ shows a quite similar behavior of our R₁₀₀, which is not surprising being quite similar in structure and composition. Moreover, the behavior of a Pyrex glass with 0.02 wt.% of FeO (considered as impurity) [21], shows a magnetic field dependence similar to our B₁₀₀ displaying a threshold field above 2T but again, without any low-temperature upturn worth of note. Thus, such a behavior, in particular that of B₁₀₀, has not been documented in any silicate systems to date.

Nevertheless, such low- T upturn, was seen only in alloys and materials exhibiting ferromagnetism [22–24] and described by means of either spin fluctuation [11] or magnetic clusters [12,13]. In order to confirm that the peculiar behavior is of magnetic origin, the field dependence of the heat capacity of R₁₀₀ and B₁₀₀ was studied in detail. The results from the tests with magnetic fields (up to 9 T), are presented in Fig. 2.

Fig. 2 shows the magnetic field influence on the low temperature

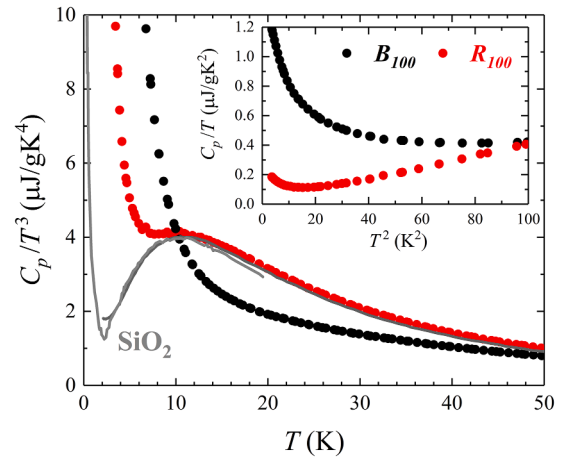


Fig. 1. C_p/T^3 vs. T plots of basaltic (B₁₀₀) and rhyolitic (R₁₀₀) volcanic glasses together with pure silica glass (SiO₂) from Ref. [18]. Inset: C_p/T vs. T^2 plot of volcanic glasses B₁₀₀ and R₁₀₀.

heat capacity of studied volcanic glasses. In both cases one can determine the initial enhancement of the additional, excess contribution to the specific heat with an increasing magnetic field up to a certain threshold value, different for each glass. In the case of B₁₀₀, the initial subsection of the sample to 1T and 2T magnetic field results in an increased anomaly at low temperatures, while further increasing of the external field gradually softens the phenomena. R₁₀₀ also shows the strongest enhancement of the behavior for a 1T and 2T field, while in this case only 5T field addition to the sample results in a final decrease of the excess heat capacity contribution. The field influence on the heat capacity was indicated by directional arrows on plots tracking the evolution of anomaly (Fig. 2). Given the above magnetic field dependence one can conclude that the anomalous C_p cannot be described within a standard disordered system approach, Eq. (1), but one should include other terms related to the magnetic contributions. Additional indications for looking beyond the standard approach are given also in Figure S2 of *Supplementary Material*, where the reduced heat capacity data still exhibits a low- T upturn. Looking at the composition of those multicomponent glasses, Table 1, (ten different oxides), sounds reasonable to ascribe this peculiar magnetically induced behavior to Fe ions. For this possible explanation the additional arguments in favor could be given by simply looking at the absolute values of heat capacity in Fig. 2. The colossal low- T upturn in the case of the B₁₀₀ is almost 4 times higher than that of R₁₀₀ which corresponds to the increased Fe content in the sample. The accurate description of the magnetic contributions to the low- T heat capacity should include two approaches:

- (i) extension of the conventional Eq. (1), by including the spin wave ($B_{3/2}T^{3/2}$) and hyperfine ($\frac{\epsilon}{T^2}$) contributions, [25,26]

$$C_p = \frac{\epsilon}{T^2} + B_{3/2}T^{3/2} + \gamma T + \beta T^3. \quad (2)$$

Another significant point here is that the linear term also includes the

Table 1

Chemical composition in wt.%, total iron oxide (FeO_{tot.}), the ratio between ferrous and total iron cations (Fe²⁺/Fe_{tot.}) expressed as Fe²⁺/Fe_{tot.} and density (ρ) of basaltic (B₁₀₀) and rhyolitic (R₁₀₀) glasses from Ref. [14].

	SiO ₂	TiO ₂	Al ₂ O ₃	FeO _{tot.}	MnO	MgO	CaO	Na ₂ O	K ₂ O	P ₂ O ₅	Fe ²⁺ /Fe _{tot.}	ρ [g cm ⁻³]
B ₁₀₀	49.71	0.76	9.51	8.86	0.16	14.53	14.64	1.80	0.03	0.01	0.386	2.757
R ₁₀₀	79.82	0.10	8.57	1.86	0.07	0.71	1.57	3.92	3.37	0.01	0.342	2.368

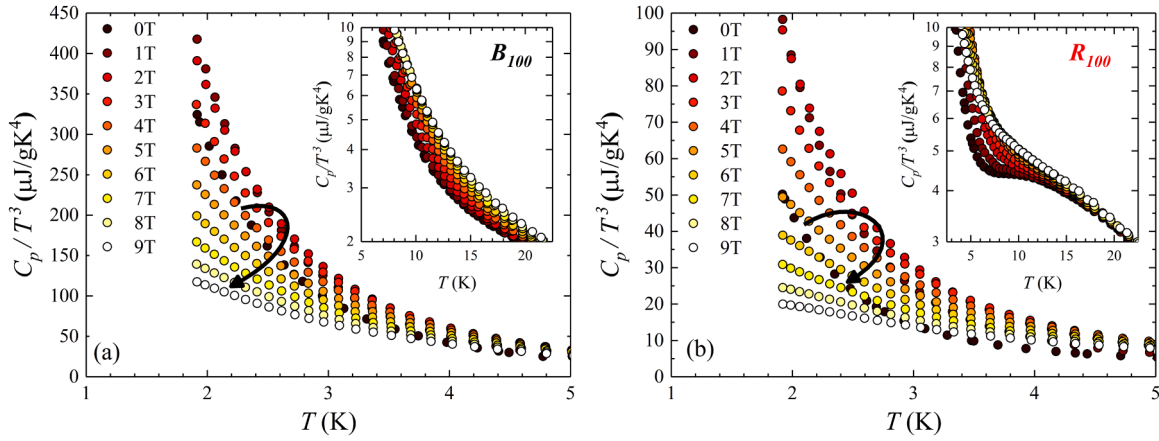


Fig. 2. Field dependent C_p/T^3 vs. T plots of volcanic glasses B_{100} , the basalt (a) and R_{100} , the rhyolite (b). Insets show a broader temperature range field influence.

electronic contribution to low- T heat capacity and there is no simple way to extract each of them.

(ii) the anomalous low- T heat capacity is the result of magnetic clusters. Here, an additional term is introduced as the excess heat capacity [23],

$$C_{\text{excess}} = A_0 \left[E\left(\frac{\theta_S}{T}\right) - E\left(\frac{N_e \theta_S}{T}\right) \right], \quad (3)$$

where $E(x) = x^2 e^x (e^x - 1)^{-2}$ is Einstein function, $A_0 = N_c \cdot k_B$, N_c is the number of clusters, defined as Fe-rich regions, $\theta_S = \varepsilon / k_B$, with ε is the energy between the levels, and their number (N_e) [23].

In order to accurately describe the volcanic glasses data at different magnetic fields, both of the approximations were tested. In the case of

the first approach – Eq. (2), the fits were introduced as short dotted lines on the plots of particular fields of Fig. 3. In the second approach, according to the magnetic clusters model, the fits are given by solid lines following the equation:

$$\frac{C_p}{T} = \frac{\alpha + \beta T^2 + A_0 \left[E\left(\frac{\theta_S}{T}\right) - E\left(\frac{N_e \theta_S}{T}\right) \right]}{T}. \quad (4)$$

The output values of the fitting parameters of Eqs. (2) and (4) are reported in Table S1 and S2 in the *Supplementary material*. In both cases the C_p was approximated disregarding the T^5 - soft modes term, as one with a very minor impact on the resulting heat capacity.

The Fig. 3 includes all applied fields in the case of B_{100} (with higher Fe content) whilst the resulting plots of the R_{100} sample are given in Fig. 4. The map of separate panels for each magnetic field was designed to visualize the changing behavior in samples.

The plots of Fig. 3 and Fig. 4 clearly show a competition-like between

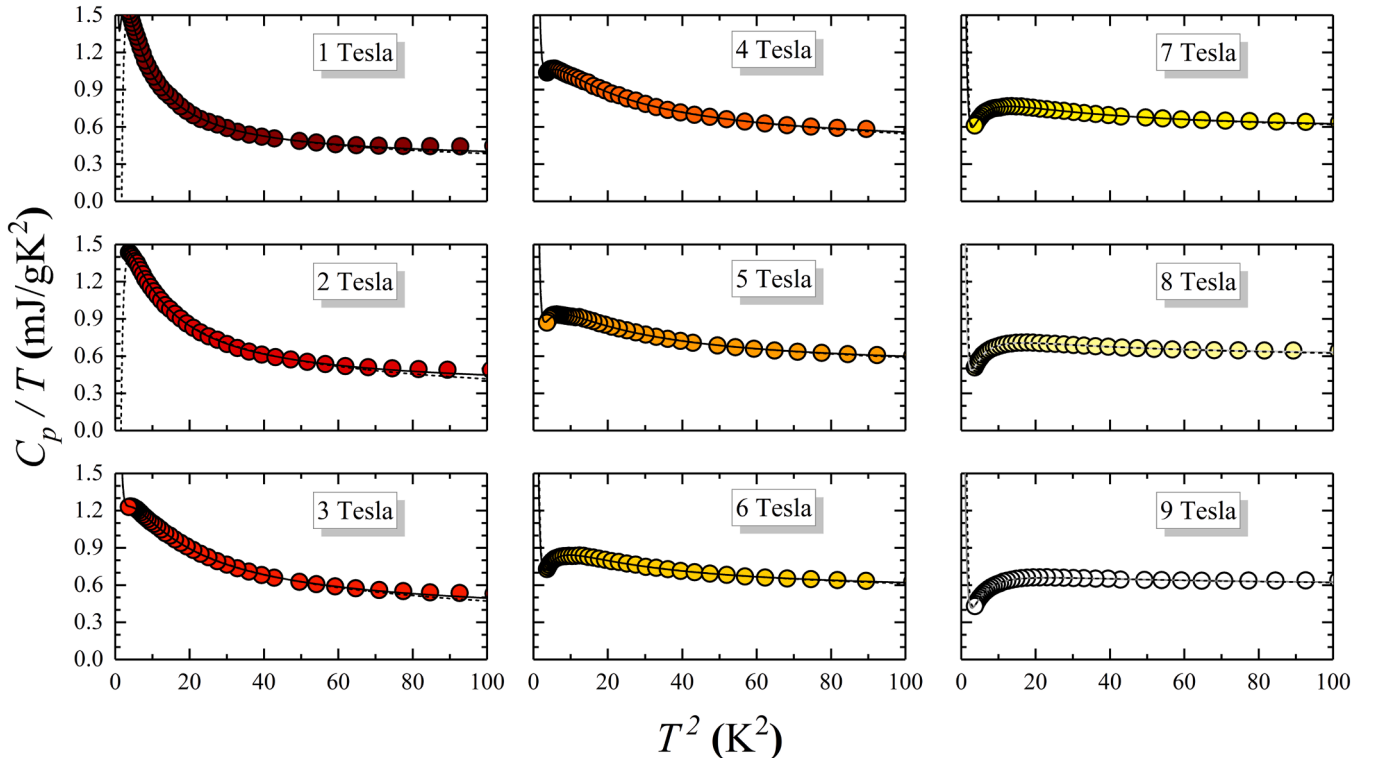


Fig. 3. The fitted C_p/T vs. T^2 plots of the basaltic glass (B_{100}) obtained under different magnetic fields.

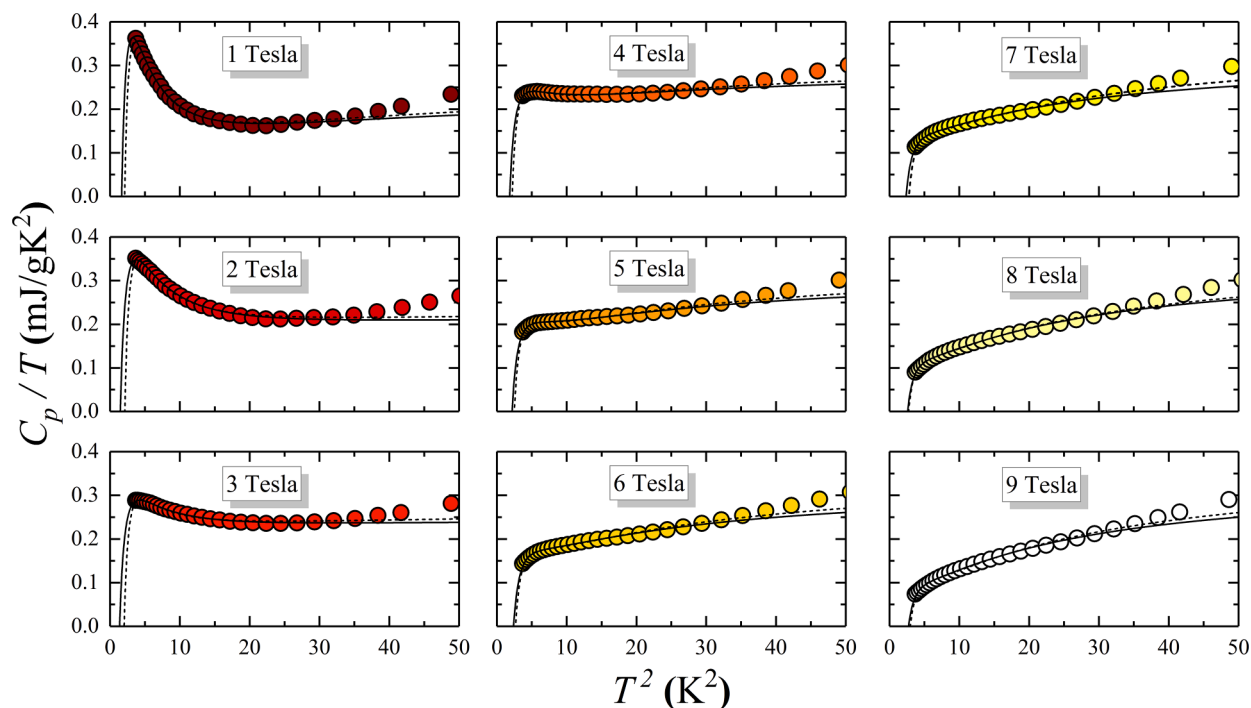


Fig. 4. The fitted C_p/T vs. T^2 plots of the rhyolitic glass R_{100} obtained under different magnetic fields.

the models Eqs. (2) and (4) in describing the two samples (see the dotted and solid lines respectively). One can almost claim that both fits work equally well as would be expected in temperatures well below the possible BP of the studied materials. In the case of the B_{100} sample the experimental data were approximated with each model below $70\text{--}75\text{K}^2 \approx 8.5\text{ K}$, for the R_{100} one, the fitting region was limited to temperatures below $35\text{--}40\text{K}^2 \approx 6\text{ K}$. The observed C_p/T^3 curves (Fig. 2) of the threshold magnetic field saturating at 2T, can also be traced on Fig. 3 and Fig. 4, and directly in the used approximation. Looking closely at output parameters of Eqs. (2) and (4), Table S1 and S2, one finds corresponding trends of particular values following the magnetic field dependence. Namely, an initial enhancement of anomalous behavior up to 2T for B_{100} and R_{100} is matching either decrease or increase of fitting parameters, followed by the reverse trend after overcoming the field threshold value, 5T for B_{100} and 3T for R_{100} respectively. Moreover, it is important to mention that only in the case of B_{100} the magnetic clusters model provided the physical parameters giving clues on the magnetic behavior standing behind the observed phenomena. In all the remaining examples, the approximation matches the experimental data with high accuracy but lacks scientific justification.

To better visualize the magnetic field evolution with the related fits we provided two gifs in the *Supplementary material*, Figure S3 and S4. Once more, including the above presented analysis we emphasize that this complex magnetic nature of investigated volcanic glasses cannot be attributed to only one particular mechanism.

4. Conclusions

Contrary to expectations, a colossal upturn at low temperature heat capacity was observed for both investigated volcanic glasses: basaltic (B_{100}) and rhyolitic (R_{100}). As a result, a conventional disordered structure approximation of the experimental data was not applicable. It revealed the existence of an excess phenomena of magnetic origin, and motivated additional studies with magnetic field dependence up to 9T. The excess heat capacity was accurately described within the known magnetic models, but the observed magnetic behavior and hence the origin of the colossal upturn was found to be of complex origin and could

not be straightforwardly assigned to only one type of mechanism (*i.e.* fluctuating spin or iron-rich clusters). In order to define the exact applicability ranges of the approximations, advanced further studies, including magnetization and susceptibility are necessary. Finally, we outline that low- T heat capacity studies offers a potentially promising and integrative approach to determine the contribution of magnetic elements in volcanic glasses (iron), in addition to its application in assessing the medium-range order of glass and possibly to provide new insights on the nucleation of nanometric iron-bearing oxides crystals.

CRediT authorship contribution statement

Daria Szewczyk: Writing – original draft, Validation, Methodology, Investigation, Formal analysis, Conceptualization. **Michele Cassetta:** Writing – review & editing, Visualization, Resources, Investigation, Conceptualization.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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Supplementary materials

Supplementary material associated with this article can be found, in the online version, at [doi:10.1016/j.jnoncrysol.2024.123046](https://doi.org/10.1016/j.jnoncrysol.2024.123046).

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